

2019年天津河东区天津市第七中学高三一模文科数学试卷(答案)

一、选择题

1. D

2. D

3. B

4. A

5. A

6. A

7. C

8. D

二、填空题

9. $[1, 3]$

10. $2\ln 2 - 2$

11. $\sqrt{6}\pi$

12. $-\frac{1}{13}$

13. 8

14. $\frac{5}{6}$

三、解答题

15. (1) $a = 14, b = 17$.

(2) $\frac{3}{7}$.

16. (1) 60° .

(2) $\frac{17 + 12\sqrt{7}}{50}$.

17. (1) 证明见解析.

(2) 证明见解析.

(3) $\frac{\sqrt{6}}{6}$.

18. (1) 是等比数列.

(2) $a_n = a^{n-1} p \frac{n^2 - 3n + 2}{2}, n \in \mathbb{N}^*$.

(3)
$$S_n = \begin{cases} \frac{n(n+1)}{2}, & p = 1 \\ -\frac{n(n+1)}{2}, & p = -1 \\ \frac{p(1-p^{2n})}{(1-p^2)^2} - \frac{np^{2n+1}}{1-p^2}, & p \neq \pm 1 \end{cases}.$$

19. (1) 椭圆的方程为: $\frac{x^2}{4} + y^2 = 1$.

(2) 直线 l 与 y 轴交点的坐标为: $\left(0, \pm \frac{\sqrt{2}}{2}\right), \left(0, \pm \frac{\sqrt{6}}{2}\right)$.

20. (1) $a = \frac{1}{3}, b = \frac{1}{3}.$

(2) $2 < a < \frac{13}{3}.$

(3) $k \in \left(-\infty, -\frac{\sqrt{21}}{7} \right) \cup \left[-\frac{1}{3}, 0 \right), G(x)_{\min} = \frac{2}{3}k^3 - 2k,$

$k \in \left[-\frac{\sqrt{21}}{7}, -\frac{1}{3} \right), G(x)_{\min} = -\frac{26}{3}k^3 + 2k.$